Numerical studies of blood flow in healthy, stenosed, and stented carotid arteries

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SUMMARY

Numerical analysis of pulsatile blood flow in healthy, stenosed, and stented carotid arteries is performed with the aim of identifying hemodynamic factors in the initiation, growth, and the potential of leading to severe occlusions of a diseased artery. The Immersed Finite Element Method is adopted for this study to conveniently incorporate various geometrical shapes of arteries without remeshing. Our computational results provide detailed quantitative analysis on the blood flow pattern, wall shear stress, particle residence time, and oscillatory shear index. The analysis of these parameters leads to a better understanding of blood clot formation and its localization in a stenosed and a stented carotid artery. A healthy artery is also studied to establish a baseline comparison. This analysis will assist in developing treatments for diseased arteries and novel stent designs to reduce restenosis. Copyright © 2008 John Wiley & Sons, Ltd.

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1. INTRODUCTION

Currently, stroke is the third leading cause of death in the United States [1] with more than 700000 Americans experiencing a stroke each year. Stenoses and occlusions of carotid arteries are involved in 34–44% of strokes [2, 3]. The development of a gradual stenosis in the arteries limits oxygen transport to tissues and dependent organs. It is believed that thrombi formed within and distal to the stenoses pose clinical threats. In the case of carotid arteries, the clinical threat is largely due

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to the embolization arising from an atherosclerotic plaque or acute occlusion of the artery and the downstream propagation of the thrombus [4].

Platelets play a vital role in initiating thrombosis within stenosed arteries. The mechanical force most relevant to platelet-mediated hemostasis and thrombosis is wall shear stress, a quantity not easily measurable in vivo. The relationship between flow in arteries, particularly the wall shear stress, and the sites where atherosclerosis develops has motivated much of the research in arterial flow in recent decades [5-10]. Shear-induced platelet activation and aggregation depend on several factors that include (1) level of shear stress, (2) spatial variation in shear stress, and (3) temporal variation in shear stress. It has been proposed that very high shear conditions $(>15 \, dyn/cm^2)$ may initiate thrombosis [11], leading to thromboembolic strokes [12–14]. Several theoretical studies have been done to predict the location of maximum wall shear stress in a stenosed artery [5-10, 15, 16]. Among these studies, Ku et al. [17] and Wootton and Ku [18] pointed out that the highest wall shear stress often occurs at the throat of a stenosis. On the other hand, it has been well accepted that blood is clotted by a cascade of coagulation proteins when it is exposed to very low shear stress [17, 19–21] or when it changes rapidly in time (factor 2) or space (factor 3) [17, 22]. Most intimal thickening occurs where the average wall shear stress is less than $10 \,\mathrm{dyn/cm^2}$ [9, 11, 23]. These conditions are likely to prevail at places where the vessel is curved, bifurcates, has a junction, a side branch, or other sudden change in flow geometry [24, 25], and when the flow is unsteady [17, 26]. The severe stenosis may also cause changes in the mechanical properties of the surrounding walls [27-32]. Various in vitro studies [33-35] have shown that regions of increased blood residence time promote fibrin thrombus formation. As a result of prolonged residence time, the platelet-rich thrombus that forms at the stenosis apex extends downstream and forms a stagnation thrombus [36-38]. The danger of a stagnation thrombus is that it may grow to several centimeters in length [38] and completely fill the stagnant flow region [35, 39]. It may eventually embolize, propagate down the arterial tree, and become lodged in a small artery or a side branch.

To reduce or remove the obstructions that block a normal blood flow, angioplasty and stents were introduced to dilate the area of arterial blockage. Despite their success and widespread use, outcomes for patients receiving stents are still hampered by thrombosis and restenosis, which occur in 20-30% of the cases following the prostheses implantation [40]. A number of medical and computational studies [41–46] suggest that relatively small disturbances in the flow such as the struts of a stent may result in significant changes in the wall shear stress.

Considering the strong correlations between the arterial wall shear stress, particle residence time, and localization of thrombus formation, quantifying these hemodynamic parameters is important in understanding the development of arterial diseases, specifically how a thrombus is initiated and promoted. Thus, the goal of this study is to adopt a feasible computational technique that can quantify these hemodynamic factors using three types of carotid arteries: healthy, stenosed, and stented. The objectives of this study are threefold: (1) to quantify and assess hemodynamic factors associated with stenosis, (2) to evaluate the mutual effect between the progression of stenosis and stenosis-induced changes in local hemodynamic conditions, and (3) to evaluate at which degree the stent can potentially induce the development of restenosis. By evaluating regional hemodynamic changes for healthy, stenosed, and stented arteries, it is hoped that the development of diseases can be better explained through the view of fluid dynamics, which may ultimately result in better prevention and treatment techniques.

In this paper, we first review the numerical algorithm, the Immersed Finite Element Method (IFEM) [47, 48], used for this study with enhanced interface treatment for rigid embedded structures

in Section 2. In Sections 3–5, we present the modeling and analysis of two-dimensional unsteady pulsatile flows in a healthy carotid artery and in stenosed and stented arteries that are most relevant in the context of thrombus formation. Finally, conclusions and remarks are presented in Section 6.

2. SIMULATION TECHNIQUE AND HEMODYNAMIC QUANTITIES

2.1. Immersed Finite Element Method

In this study, we will adopt the IFEM [47, 48] that was recently developed to solve complex fluid and deformable structure interaction problems. It has been successfully used to model various biomechanics applications including shear-induced red blood cell deformation [49], stent deployment [50], and flow in cardiovascular systems [51]. This numerical technique provides the flexibilities in handling varying shapes of embedded structures. Therefore, it can be conveniently adopted in this study where the immersed structures, i.e. stenosed and stented arteries, come in different shapes and geometries. The diameter change of a carotid artery during a cardiac cycle is observed to be minimal, approximately 5–10% with a high degree of stiffness. Therefore, rigid artery walls are assumed in this study. However, if different material properties are to be considered for stenotic arteries, this numerical technique can be easily used to accommodate the deformability in stenotic arteries and their corresponding influences in the fluid flow.

In the IFEM algorithm, two sets of domains are considered: a solid structure with Lagrangian description and an incompressible fluid domain (or background grid) with Eulerian description. This setup allows us to generate fluid and solid meshes and solve fluid and solid equations independently, thus avoiding frequent mesh updating schemes. The embedded solid can move freely within the fluid domain. The interactions between the fluid and the solid are computed through interpolations of velocities and forces at the fluid–structure interface.

The no-slip boundary condition at the interface ensures the solid velocity at the solid boundary to be equal to the surrounding fluid velocity. When dealing with a rigid structure the interaction force acting on the solid structure $\mathbf{f}^{\text{FSI},\text{s}}$ can be calculated using the opposing force that is induced by the surrounding fluid such that

$$\mathbf{f}^{\text{FSI},s} = \rho \left(\frac{\partial \mathbf{v}^{s}}{\partial t} + \mathbf{v}^{s} \cdot \nabla \mathbf{v}^{s} \right) + \nabla p^{s} - \mu \nabla^{2} \mathbf{v}^{s}$$
(1)

where \mathbf{v}^{s} and p^{s} are the solid velocity and pressure on a solid boundary node \mathbf{X}^{s} , which are interpolated from the known surrounding fluid velocities and pressure. Details of the interpolation process are given in [52]. It must be noted that this force is evaluated only at the interface since there is no internal force generated inside a rigid solid.

The interaction force $\mathbf{f}^{\text{FSI},s}(\mathbf{X}^s, t)$ is then distributed onto the nodes in the fluid domain $\mathbf{f}^{\text{FSI}}(\mathbf{x}, t)$ using an interpolation function that was used as the shape function in one of the meshfree methods called Reproducing Kernel Particle Method [53, 54]:

$$\mathbf{f}^{\text{FSI}}(\mathbf{x},t) = \int_{\Omega} \mathbf{f}^{\text{FSI},s} \Phi(\mathbf{x} - \mathbf{x}^s) \,\mathrm{d}\Omega \tag{2}$$

where $\Phi(\mathbf{x} - \mathbf{x}^s)$ is the interpolation function that is defined as a function of the distance between a solid node at position \mathbf{x}^s and its surrounding fluid nodes at \mathbf{x} . Once distributed onto the fluid

domain, this interaction force serves as an external force in the fluid domain. Fluid velocities \mathbf{v} and pressure p are then solved iteratively from the Navier–Stokes equations:

$$\rho^{f}(\mathbf{v}_{,t} + \mathbf{v} \cdot \nabla \mathbf{v}) = -\nabla p + \mu \nabla^{2} \mathbf{v} + \mathbf{f}^{FSI}$$
(3)

$$\nabla \cdot \mathbf{v} = 0 \tag{4}$$

These equations are solved repeatedly for every time step with a semi-explicit time integration scheme. The accuracy of this method has been extensively studied in [52].

2.2. Fluid quantities in arterial flow

Three important hemodynamic quantities will be examined in this study: (1) wall shear stress, (2) oscillation shear index (OSI) that measures the direction of the wall shear stress, and (3) particle residence time that measures the average time that a particle (platelet) remains in a region.

The wall shear stress, τ_w , is computed from the instantaneous velocity vector field **v** as follows:

$$\tau_{\rm w} = -\mu \frac{\partial \mathbf{v}}{\partial r} \tag{5}$$

where r is the distance from the wall in the transverse direction of the flow. In numerical simulations, the wall shear stress is measured at a layer near the wall inside the channel (at around 0.01 mm apart from the wall).

The OSI is formulated to account for the cyclic departure of the wall shear stress vector from its predominant axial alignment. It is calculated on the basis of its standard definition [20] as

$$OSI = \frac{1}{2} \left(1 - \frac{\left| \int_0^T \tau_{\mathbf{w}} dt \right|}{\int_0^T \left| \tau_{\mathbf{w}} \right| dt} \right)$$
(6)

where T is the duration of the cycle and τ_w is the instantaneous shear stress. This index represents a measure of the shear stress acting on the luminal surface due to either cross flow or reverse flow that occurs in a pulsatile flow. It describes the degree of deviation of the wall shear stress from its average direction. This index may not describe the pattern (e.g. frequency, intermittence) of oscillation, but rather shows the significance of oscillations in a flow. The maximum OSI can reach 0.5. In the regions where OSI value is near 0.5, the wall is subjected to high oscillating shear stresses. In regions of unidirectional flow, OSI reaches zero.

A characteristic dimensionless residence time, T_r , of a fluid particle in the vicinity of an irregular surface is correlated with the wall shear stress and can be estimated according to Himburg *et al.* [55] as

$$T_{\rm r} \sim \frac{\mu}{T} [(1 - 2\,{\rm OSI})\langle \tau_{\rm w} \rangle]^{-1} \tag{7}$$

where $\langle \cdot \rangle$ represents the time-averaged quantity. In this definition, OSI acts to include the effect of time-averaged shear stress on the residence time at a site. When the OSI is small, it has little effect on the residence time, but as it approaches its limit of 0.5, it can have an increasingly important influence on this quantity. Using the techniques presented above, it is possible to evaluate precisely where and how long particles will reside within a given configuration.

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3. HEALTHY ARTERY

We first consider a straight two-dimensional artery with two walls separated by a distance of d=0.5 cm. The artery walls are L=5.0 cm long and t=0.07 cm thick embedded in a fluid domain of length L=5.0 cm and width D=0.8 cm as shown in Figure 1. A thinner mesh is used near the walls to ensure accuracy at the interfaces.

Pulsatile flow is considered, where the inflow velocity is based on a time-dependent flow rate Q obtained from the experiments of Holdsworth *et al.* [56] as shown in Figure 1. The waveform has a period T = 0.9 s (67 beats per minute), where 0 s < t < 0.4 s is systolic and 0.4 s < t < 0.9 s is diastolic. The maximum systolic velocity is 117.35 cm/s and the time-averaged velocity is 30.69 cm/s. Blood is considered to be homogeneous and incompressible with a constant density $\rho^{f} = 1.055 \text{ g/cm}^{3}$ and viscosity $\mu = 0.035 \text{ dyn s/cm}^{2}$. The maximum Reynolds number, given by $Re_{(max)} = \rho du_{max}/\mu$, is 1769 and the inlet pulse has a mean Reynolds number of 463. A critical parameter in this analysis is the Womersley number, defined as $\alpha = r(\omega/\nu)^{1/2}$, where ω is the angular frequency of the driving pulse, r is the radius of the vessel, and ν is the kinematic viscosity of the blood. For this given blood flow, a Womersley number of 3.63 is observed. A summary of the parameters is given in Table I. These parameters are also in agreement with physiologic observations, which for a medium-sized artery have a Reynolds number of typically on the order of 100–1000 and a Womersley parameter that ranges from 1 to 10 [57].

The results reported in this paper are obtained during the third time period, i.e. 1.8 s < t < 2.7 s, when the flow has reached a stable periodic solution. Velocity profiles at six different time steps



Figure 1. Pulsatile flow in a healthy carotid artery: (a) schematic of pulsatile flow in a healthy carotid artery and (b) flow rate from Holdsworth *et al.* [56].

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Parameters	Value
Blood density: ρ^{f}	$1.055 \mathrm{g/cm^3}$
Blood dynamic viscosity: μ^{f}	$0.035 \mathrm{dyns/cm^2}$
Blood pulse period: T	0.9 s
Artery diameter: d	0.5 cm
Artery length: L	5 cm
Artery thickness: t	0.07 cm
Maximum inflow velocity: <i>u</i> max	117.35 cm/s
Mean inflow velocity: \bar{u}	30.69 cm/s
Maximum Reynolds number: $Re_{(max)}$	1769
Mean Reynolds number: \bar{Re}	463
Womersley number: α	3.63

Table I. Carotid artery flow parameters.



Figure 2. Velocity profiles in a straight rigid carotid artery during a cardiac cycle.

during the pulsation are shown in Figure 2. As expected for this Womersley number, the inertial force dominates. The velocity profiles turn into plug flow shapes and the centerline velocity oscillates with the driving pulse. At the end of systole (t = 2.2 s), blood flow changes direction near the boundary layer due to the effect of viscous forces. These forces influence the velocity profiles in a way that, when the pressure gradient reverses, the flow near the wall changes direction. This flow behavior is in agreement with the results presented by Berbich *et al.* [58].

Correspondingly, the wall shear stress varies and oscillates with the cardiac cycle because of the pulsatile changes in the velocity and direction of the blood flow. From our computational results, we obtain a mean-average wall shear stress (the temporal mean over the cardiac cycle and the spatial average along the wall) of 8.11 dyn/cm^2 and a peak wall shear stress of 36.55 dyn/cm^2 .

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Parameters	Peak wall shear stress	Mean-average wall shear stress
IFEM	36.55	8.11
Dammers et al. [59]	34.0 ± 8.0	11.5 ± 2.1
Samijo <i>et al.</i> [65]	33 ± 6.8	12 ± 1.8
Oshinski et al. [63]		8.0 ± 4.1
Gnasso et al. [60]	29.5 ± 8.2	12.1 ± 3.1
Gnasso et al. [61]	18.7 ± 4.1	15.3 ± 4.0
Hoeks et al. [62]	22.4	7.0
Oyre et al. [64]	25.6	9.5

Table II. Summary of wall shear stress measurements in carotid arteries (units in dyn/cm²).

We compared our results with a collective experimental measurement of mean-average and peak wall shear stresses gathered from References [59–65] in Table II. The computed mean-average and peak wall shear stresses are in good agreement with these previous experimental results.

4. STENOSED ARTERY

Stenosed (constricted) arteries with varying severities of stenosis under physiologic conditions are studied in this section. The computational model and properties are built based on the healthy artery detailed in Section 3. A symmetric constriction is imposed at the center of the artery far from the outlet so that the flow can return to a nearly fully developed state and the outlet boundary does not influence activities occurring upstream. In clinical medicine, the severity of stenoses is commonly defined as the percentage of occlusion using diameter measurements: % stenosis = $(d_1 - d_2)/d_1 * 100\%$, where d_1 is the artery diameter and d_2 is the constricted diameter. As the disease advances, the percentage of stenosis also increases. Two separate studies will be performed. We first consider a stenosed artery with a moderate 50% stenosis, as depicted in Figure 3, where detailed hemodynamic parameters will be analyzed. Second, we will examine the effects of the fluid quantities with varying severities of stenosis, from mild to severe (40–76%).

4.1. Analysis of a moderate stenosis (50%)

4.1.1. Velocity. The X-component of velocity contours at different instances over one cardiac cycle is shown in Figure 4. The constriction generates a fluid jet velocity profile during systole (1.8 s < t < 2.2 s). In this jet region, the flow is accelerated with a high forward flow in the axial direction. During diastole (2.2 s < t < 2.7 s) deceleration of fluid velocity and large recirculating zone is observed downstream of the stenosis. There is also a near stagnation zone at the foot of the stenosis and several eddies form downstream of the stenosis. Similar results were observed by Rosenfeld and Einav [66]. The velocity profiles at different locations along the channel are plotted in Figure 5. In the downstream of the stenosis ($X \ge 2.65 \text{ cm}$), the flow decelerates and reverses near the wall, as they are most obviously observed in Figure 5(c-f). The presence of a constriction in the artery alters the pulsatile velocity waveforms by blocking higher frequencies and blunting the amplitude at the end of systole.

4.1.2. Shear stress. These complex changes in blood velocities can create significant changes in the wall shear stress. Figure 6 shows the wall shear stress during one cardiac cycle at different



Figure 3. Pulsatile flow in a constricted carotid artery.



Figure 4. Velocity contours in a moderate (50%) stenosed artery during a cardiac cycle: (a) systole and (b) diastole.

locations around the constriction. The wall shear stress increases sharply at the upstream of the constriction (points 3–5). The peak value is identified at the tip of the constriction (point 5) at the end of systole. On the other side of the constriction and during diastole, low wall shear stress is observed (points 7 and 8). Around the constriction, we observe a maximum value of the wall shear stress $\tau_{wall(peak)}$ to be 388 dyn/cm² and a time-averaged value $\tau_{wall(mean)}$ of 93.8 dyn/cm² near the throat (at an angle of ~78°) (Figure 6), which are in the physiologic range as reported in [13, 67]. Studies from Holme *et al.* [68] and Sakariassen *et al.* [69] concluded that a shear stress threshold of 315 dyn/cm² is sufficient to induce significant platelet activation and micro-particle formation. Thus, our results suggest that the sudden spatial change (stenosis) increases the wall shear stress dramatically compared with a healthy artery where the shear stress is found to be 36.55 dyn/cm² from the previous study in Section 3. This high wall shear stress might be an important factor for activation and thrombus formation for a moderate stenosis.

4.1.3. Oscillatory shear index. In the downstream of the stenosis (X > 2.65 cm), the strong unsteady flow causes a corresponding unsteadiness in the wall shear stress field. The mean wall shear stress is found to be very low and oscillating between positive and negative values along the longitudinal direction as plotted in Figure 7. This oscillatory behavior of shear stress is best represented by

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Figure 5. Velocity profiles at different locations in a moderate (50%) stenosis during a cardiac cycle: (a) X = 2.0 cm; (b) X = 2.5 cm; (c) X = 2.65 cm; (d) X = 3.5 cm; (e) X = 4.0 cm; and (f) X = 4.8 cm.



Figure 6. Wall shear stress at different locations around a moderate (50%) stenosis during one cardiac cycle: (a) wall shear stress during a cardiac cycle and (b) mean and peak wall shear stresses around a moderate (50%) constriction.

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Figure 7. Arterial flow quantities (mean wall shear stress, oscillatory shear index, and residence time) at downstream of a moderate (50%) constriction: (a) mean wall shear stress; (b) oscillatory shear index; and (c) residence time.

a parametric study of the OSI. The OSI is examined at around the stenosis and downstream of the flow as shown in Figure 7. Around the stenosis a low and decreasing OSI is observed, while downstream a very high OSI appears with a maximum value of 0.44, which means that the wall is subjected to high oscillating shear stress or regions of flow reversal. By investigating the distribution patterns of mean wall shear stress and OSI in relation to the features of the intravascular flows, it is easy to find that the low mean wall shear stress and high OSI regions coincide well with the regions where flow separations are present. Longest and Kleinstreuer [70] suggested that regions exposed to a high OSI are more susceptible to plaque formation, which in our model would be downstream of the constriction.

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4.1.4. Residence time. The last hemodynamic parameter under investigation in the current study is the residence time. The probability of a given platelet triggering a thrombus formation depends on the residence time available for platelet activation and on the local wall shear stress. Since the region immediately downstream of an arterial stenosis induces an abrupt reduction in wall shear stress and low reversing velocities, local residence time may be an important factor in determining degrees of stenoses and types of flow conditions that might be most conducive to platelet adhesion. The computed residence time downstream of the stenosis is presented in Figure 7. During diastole, the deceleration and reversal of flow downstream of the stenosis with the presence of a weak forward jet and large recirculation zones lead to extended particle path lengths and greater residence times. With a high residence time, activated platelets may recirculate in the separated region long enough to form small aggregates. Our results agree with the simulation studies obtained from Kunov *et al.* [71] who quantified platelet residence times in the region of an axisymmetric 45% area reduction stenosis.

4.2. Analysis of varying degrees of stenosis (40–76%)

The severity of stenosis is an important determinant of the wall shear stresses, OSI, and particle residence time. We conduct our study for mild (40%), moderate (50, 60%), and severe (70, 76%) stenoses with a smooth symmetric plaque surface morphology.

4.2.1. Velocity. For all degrees of stenosis, a relatively large recirculation region is found to exist downstream of the constriction (Figure 8). This figure shows that increasing the size of a constricted region corresponds to increasing number of vortices with higher strength. These recirculation zones are indications of regions where the flow is reversed in a significant portion of each cycle.

4.2.2. Shear stress. The severity of the stenosis affects the shear stress characteristics significantly, especially at the tip of the stenosis. There is a very significant increase in shear stress with increasing level of severity of stenosis. We found that for the most severely stenosed case, the magnitude



Figure 8. Velocity contours of flows in varying degrees of stenosis.





Figure 9. Mean-average wall shear stress of the constriction as a function of degree of stenosis.

of the peak value reaches more than 14 times of the unstenosed case found in Section 3, similar to clinical observations that are reported in [22]. The mean-average (the temporal mean over the cardiac cycle and the spatial average along the wall) wall shear stress is shown in Figure 9. An interesting result is that the wall shear stress does not increase linearly with the degree of stenosis. It increases sharply at around 70% occlusion. The *in vivo* study by Merino *et al.* [72] showed that although platelets formed a mural thrombus in all the vascular injury models, which ranged from 0 to 92% stenosis, the thrombus progressed to occlusion only if the stenosis severity was greater than 60%. Our results suggest a similar phenomenon where an occlusion of more than 70% of the artery may result in dangerous medical condition for its rapid increase in the wall shear stress. Regions of low and oscillating wall shear stress persist in the downstream regions of the constriction as the degree of the stenosis increases as shown in Figure 10. For mild (40%) stenosis, the oscillations are quickly washed out and the low (negative) wall shear stress region is concentrated in the vicinity of the root of the constriction. As the stenosis grows, oscillations and low shear regions develop further downstream.

4.2.3. Residence time. As the degree of stenosis increases, up to 76%, the location of maximum residence time is located farther and farther from the constriction as shown in Figure 10. The magnitude of residence time increases for up to 60% stenosed arteries. Then, for higher degrees of stenosis, the residence time decreases and reaches a very low value at 76%. This result shows that the particle residence time does not correlate proportionally with the degree of stenosis. For high degrees of stenosis, platelets tend to be washed out faster by rapidly changing flow and particle residence time is shorter. It is safe to conclude that the growth of intima will not be exacerbated by the particle residence time after the lesion is formed because the particle residence time appears to reduce at high degrees of stenosis.

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Figure 10. Mean wall shear stress and residence time downstream of the constriction for varying degrees of stenosis: (a) mean wall shear stress and (b) residence time.

5. STENTED ARTERY

We now consider the flow in a vessel where an interventional device such as a stent is inserted. A stent, a wire frame used to support the artery, is very effective in opening up the lumen in a stenosed vessel. The study of blood flow dynamics is very complex around the wall where the stent in deployed because many mechanical and geometric characteristics are involved. Thus, it is necessary to simplify the model while maintaining reasonable physiologic conditions. We first assume that the artery has a constant length and diameter. The model geometry includes only the wire structure and the vessel wall. No consideration is given to the appearance of thrombus that can occur within minutes to hours after stent implantation. The stent strut is $\lambda_s = 0.008$ cm in thickness and $t_s = 0.008$ cm wide. Each strut is separated by 0.03 cm from each other. The stent considered in this model is $L_s = 0.8$ cm long with 22 identical struts and implanted at X = 2.0 cm from the entrance of the artery as shown in Figure 11. The fluid model, boundary, and initial conditions and properties are the same as the ones detailed in the previous flow in carotid artery examples.

5.1. Velocity

A velocity vector plot between two adjacent stent struts (near the eighth stent strut) at different periods of the cardiac cycle is shown in Figure 12. Large fluid perturbations start to appear at the tip of the strut. A clockwise vortex with a low magnitude forms at the beginning of diastole (t = 2.05 s) and disappears at the end of diastole (t = 2.20 s). This slow moving vortex is destroyed rapidly by reversing flows. The velocity of this vortex is very small compared with the velocity observed above the stent wires. For instance, at the end of systole, the velocity in the mainstream (centerline of the artery) is approximately 41.6 cm/s. However, the maximum velocity within the recirculation zone is 1.49 cm/s or about 3.5% of the maximum velocity. This is in agreement with previous results [46, 73]. Thus, these flow patterns should not be viewed as strong vortices, but rather as zones of stagnation.

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Figure 11. Pulsatile flow in a stented carotid artery.



Figure 12. Velocity vector plot inside a stented region during a cardiac cycle.

5.2. Shear stress

We now quantify the wall shear stress between the stent branches. For the most part of the unstented region, the mean-average wall shear stress value is $8.47 \,\text{dyn/cm}^2$, which agrees with our previous result in Section 3. In the stented region, we observed a significant decrease along the inner strut wall in the mean and peak space-dependent wall shear stress distribution shown in Figure 13. A low mean shear stress zone (< $5.0 \,\text{dyn/cm}^2$) is observed in between stent struts. A mean-average value of $5.32 \,\text{dyn/cm}^2$ is found in between the stent struts. Higher shear stress values are found on or near the stent struts where the maximum mean shear stress measured in this region is $18.01 \,\text{dyn/cm}^2$. The peak wall shear stress measured at the end of systole ranges between 13 and $108 \,\text{dyn/cm}^2$. Our numerical results compared quite well with those reported by Benard *et al.* [45], which had $15 \,\text{dyn/cm}^2$ for shear stress measured near a stent strut, and Wentzel *et al.* [43] who found wall shear stress from simulations varying from 3 to $90 \,\text{dyn/cm}^2$.

In most stents, the site with the greatest stress concentration is at the entrance of the stent. This is particularly apparent in our model as shown in Figure 14 where high or low wall shear stress



Figure 13. Mean and peak wall shear stresses inside one central strut of the stent.



Figure 14. Shear stress contours along the stent and artery wall with zoomed entrance and exit of the stented region.

is observed at the ends of the stent. In the central part of the stented area, the pattern detailed previously appears repetitively. The fluid–structure interaction between the stent wire and the blood flow alters the wall shear stress at the entrance and the exit. At the entrance, it shows a remarkably high wall shear stress concentration of $212.5 \, dyn/cm^2$. At the exit, a large low and oscillating wall shear stress area forms behind the stented region.

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Figure 15. Oscillatory shear index and residence time along the stented region: (a) oscillatory shear index and (b) residence time.

5.3. Oscillatory shear index

The OSI distribution along the stented region is presented in Figure 15 to characterize the transient nature of arterial flow fields. The corresponding stent is drawn at the bottom of the figure to identify the regions with minimum and maximum values. For struts located in the middle of the stent, OSI sharply increases to an average value of 0.23 in between struts. At both ends, the OSI reaches maximum values of 0.42 at the entrance and 0.33 at the exit of the stented region. This means that the wall is subjected to high oscillatory shear stresses at both ends, while at the center of the stented region the oscillatory behavior of the wall shear stress is diminished. From the analysis of the OSI, we can conclude that the flow reversal between each strut depicted in Figure 12 is more important at the entrance and around the last strut of the stented region.

5.4. Residence time

The characteristic residence time along the stented region is evaluated as shown in Figure 15(b). The residence time is much higher at the entrance (first strut) and the exit of the stent. A particle is twice more likely to be trapped in a strut at the entrance and/or at the exit of the stented region than at any other centered strut of the stent.

According to our results, it is likely that the platelets are activated at the entrance of the stent due to high wall shear stress and high OSI. We then observe repetitive patterns for velocity and wall shear stress along the stented region, characterized by flow recirculation and low wall shear stress. Since most intimal thickening occurs where the average wall shear stress is less than 5.0 dyn/cm^2 , the whole stented region presents restenosis risk for all surfaces close to stent wire. The exit, which has a high residence time, may be a favorable spot for adhesion and accumulation of platelets. This higher blood residence time increases the exposure time of blood elements and provides an environment prone to thrombosis. The *in vitro* studies of Sprague *et al.* [74], with cell growth in stagnation zone and along the stent strut, corroborate our numerical results.

6. CONCLUSIONS

Blood flow in idealized physiologic vascular models of healthy, stenosed, and stented carotid arteries was simulated and studied quantitatively. The hemodynamic quantities such as the velocity profiles, shear stress, OSI, and particle residence time were analyzed for stenosed and stented arteries using the IFEM. A healthy artery was first studied to establish a baseline comparison. The diseased and stented arteries are found to have significantly higher and oscillating wall shear stresses than a healthy artery. In a stenosed artery, we found a high wall shear stress at the stenosed throat, a low and oscillating wall shear stress downstream of the stenosis, and a high residence time immediately downstream of the stenosis. In the stented artery, the wall shear stress and the residence time are the highest at the entrance and the exit of the stent, while they decrease significantly in between stent struts. The results suggested that platelets/particles are most likely to be activated near the entrance; they form aggregates in between struts where the shear stress is very low and eventually reside at the end of the stent where the residence time is the highest. The simulations and analysis presented in this paper will be helpful for defining biomarkers and obtaining optimal stent designs, which can potentially minimize hemodynamic effects prone to thrombosis. Optimizing the shape and geometry of these types of medical devices to minimize unfavorable fluid mechanical effects will contribute to the prevention and intervention of serious cardiovascular diseases.

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