

## GEOMETRIC MODELING AND ITS RELATIONSHIP TO F.E. MODELING

### Background:

Goal of FEA is to solve some set of partial differential equations over a given domain

Geometric model is computerized representation of domain

### State-of-the-art:

Several technologies to support the complete and unique computerized definition available

Range of geometry types available is constantly improving - NURBS are becoming standard

Geometric modeling systems providing better support for applications

Geometric modeling systems integral part of the engineering design process

Geometric models used form conceptual design through manufacturing

## TERMINOLOGY

Geometric Modeling - Collection of procedures and representations for construction and description of the shape and spatial relations of objects  
Wireframe Modeling - Collection of curve definitions for the edges that bound an object

Surface Modeling - Collection of curve and surface definitions for the edges and faces that bound an object

Solid Modeling - Complete & unambiguous computerized representation of objects. There are six known families of unambiguous schemes  
Constructive Solid Geometry (CSG) - Solid modeling approach where object is constructed by Boolean set operators

Boundary Representations (B-reps) - Solid modeling approach where the boundary, along with sufficient associatively information are stored

Topology (with respect to geometric modeling) - An abstract representation of the associations of the objects boundary entities

Manifold (2-manifold) Solid Representations - Every point on a surface has a neighborhood which is homeomorphic to a two-dimensional disk

Non-Manifold Geometric Modeling - Allows situations which are not 2-manifold. Allows wire edges, dangling surfaces, and more than two faces to an edge

## APPROACHES TO THE INTEGRATION OF MESH GENERATION AND GEOMETRIC MODELING

No Interface - Generate geometry in the finite element modeling system

Static Geometric Interface - Standard file format used for the geometry

Dynamic Geometric Interface - The functionality of the geometric modeling system used by the application programs

No interface forces the re-definition of desired geometry

A static interface provides geometry, but the mesh generator must reproduce the needed geometric modeling functions. Also lose control of geometric approximation issues

### DYNAMIC INTERFACE

Directly provides the geometric modeling functionality needed

Supports both geometric interrogation and geometric modification

Can support geometric approximation issues

Topological entities and associativities provide ideal means for coordinating a dynamic interface

Boundary topology provides:

- A shape independent abstraction
- A unique representation
- A natural method since most focus is on the object's boundary

## INTEGRATION OF APPLICATIONS WITH GEOMETRIC MODELER

Data exchange standards provide substantial capability

Dynamic interfaces required to effectively support applications like automatic mesh generation

Need the combination of PDES/STEP and the CAM-I Applications Interface Specification

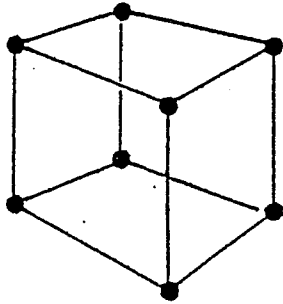
### EXAMPLE DYNAMIC INTEGRATION: FINITE OCTREE

Finite Octree:

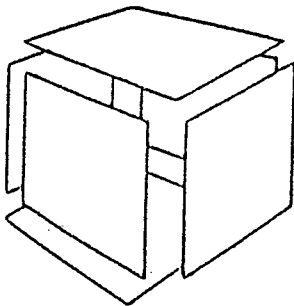
- Automatic 3-D mesh generator
- Integrates with a geometric modeler via 21 operators - no knowledge of modeler data used
- Approx. 1/2 the operators request topological adjacencies - e.g. the vertices of an edge
- Approx. 1/2 are pointwise interrogations - e.g. line/surface intersection, surface normal

Finite Octree has been linked with systems including Parasolids, Shapes and ACIS

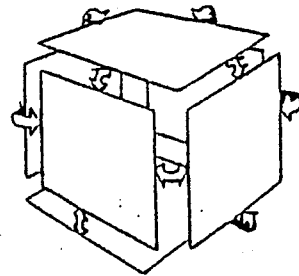
Modeling system supported a library with needed interrogations



WIREFRAME

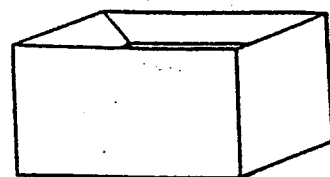
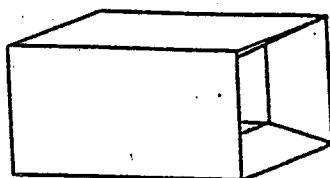
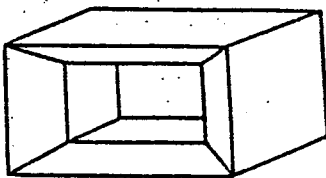
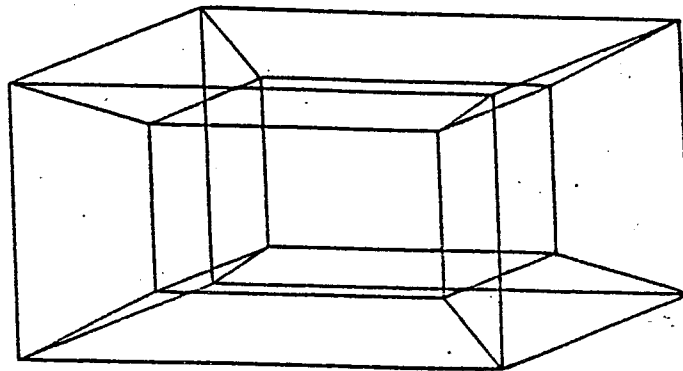


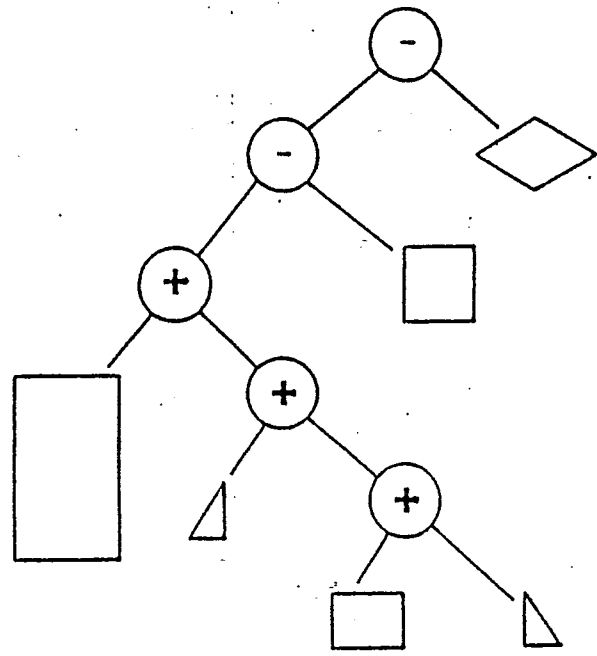
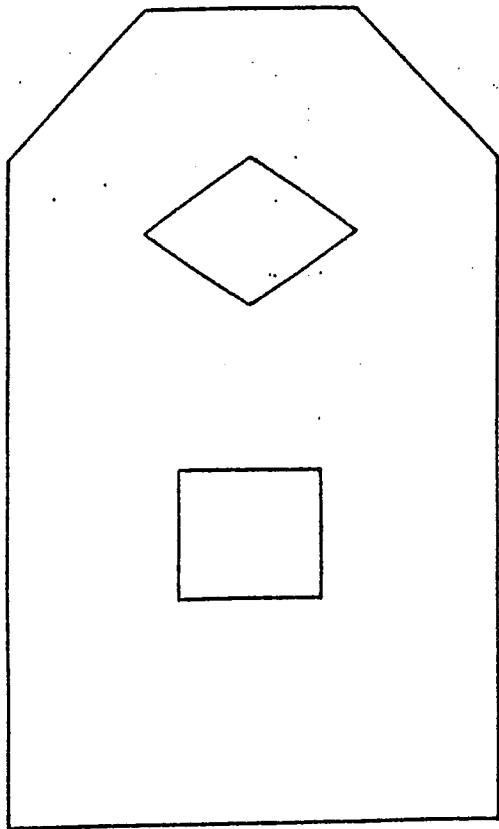
SURFACE



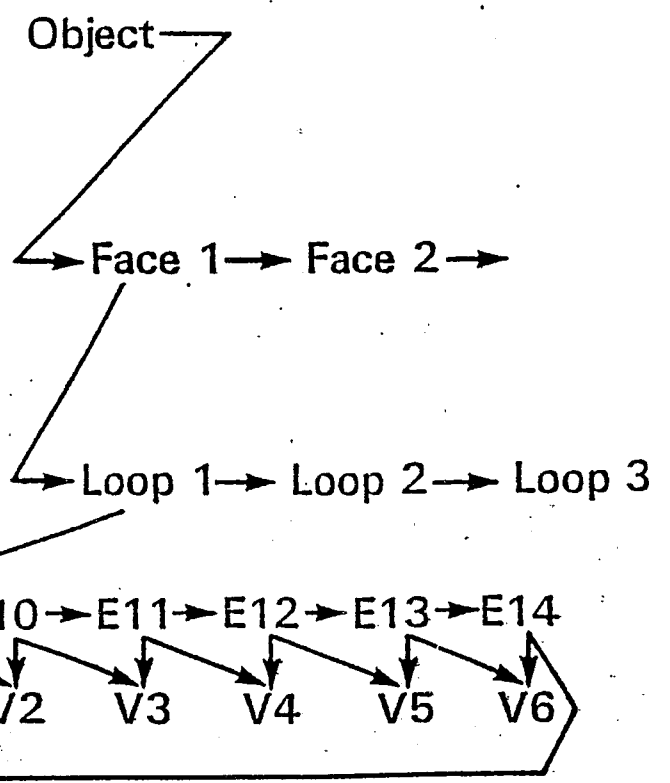
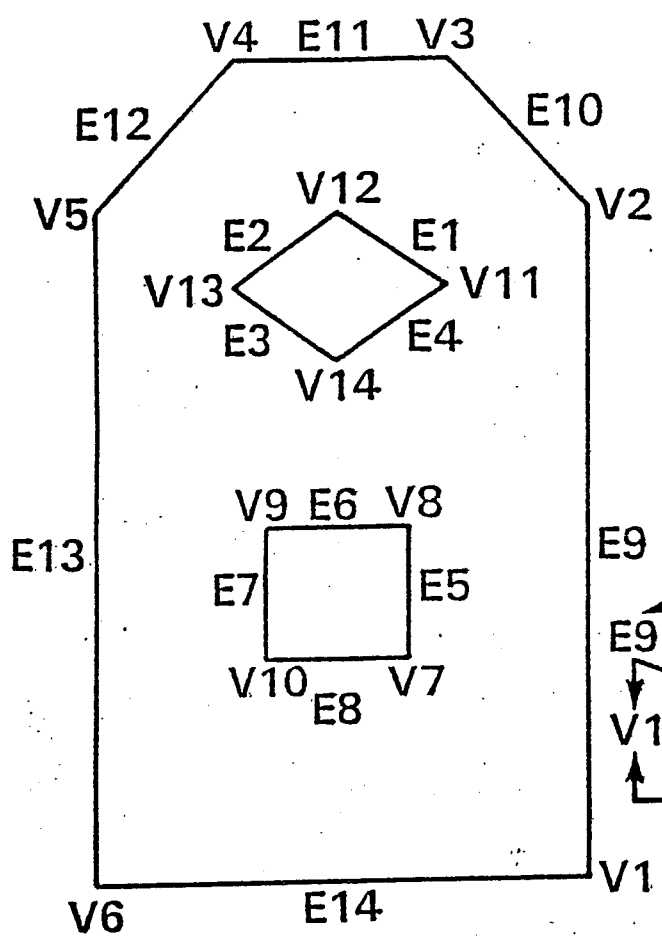
SOLID

## Ambiguous Geometry

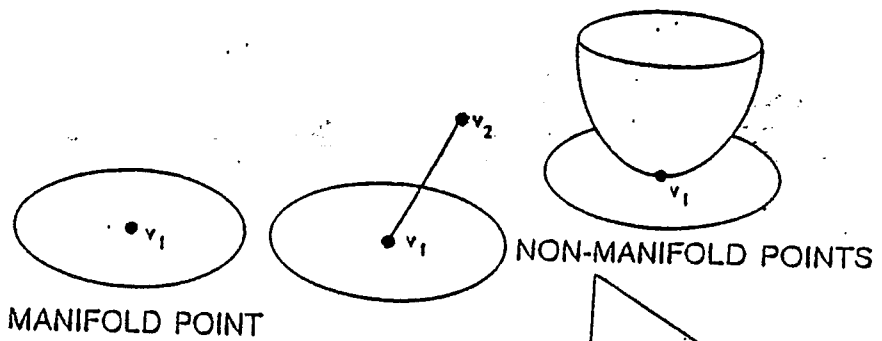




CONSTRUCTIVE SOLID GEOMETRY

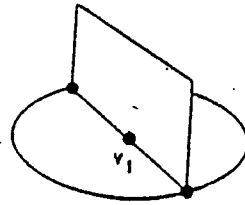
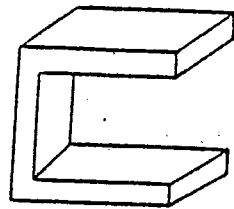


BOUNDARY REPRESENTATIONS

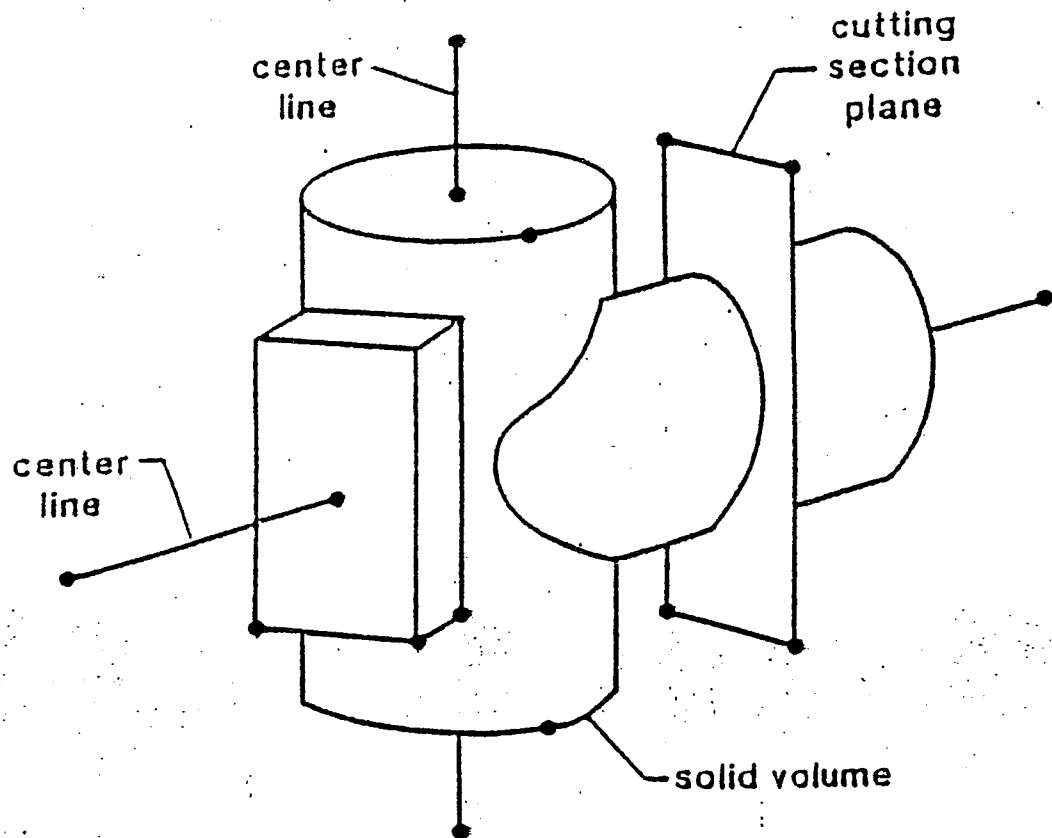
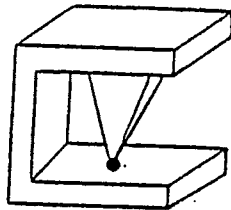


MANIFOLD POINT

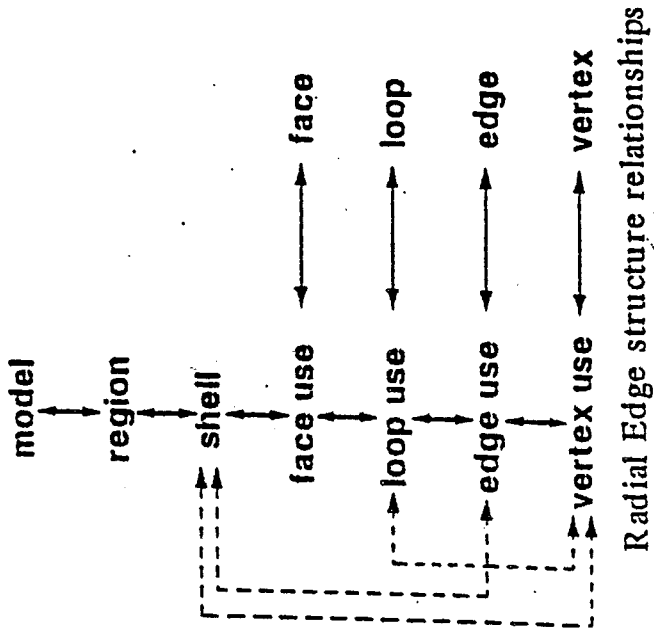
NON-MANIFOLD POINTS



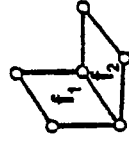
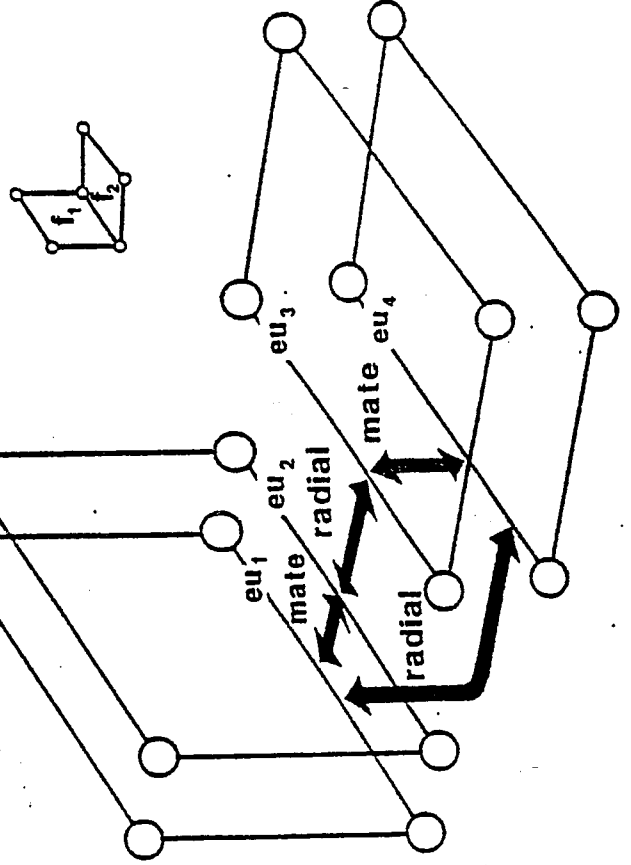
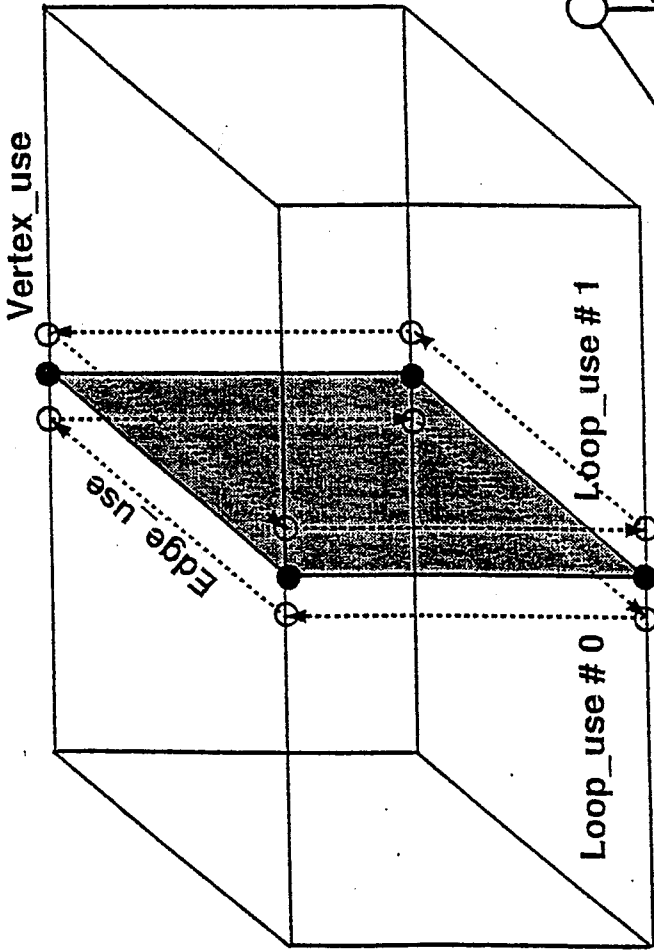
NON-MANIFOLD RESULT FROM UNION OF TWO MANIFOLD OBJECTS

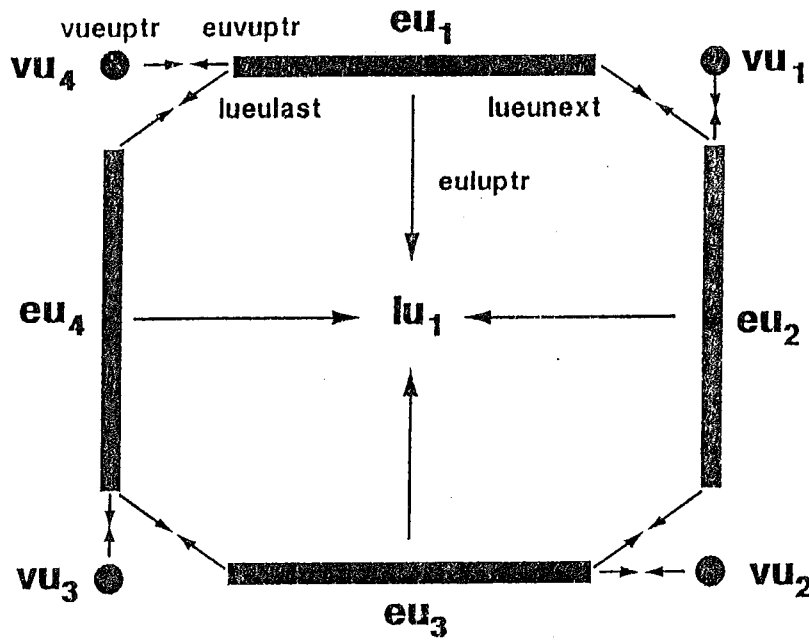
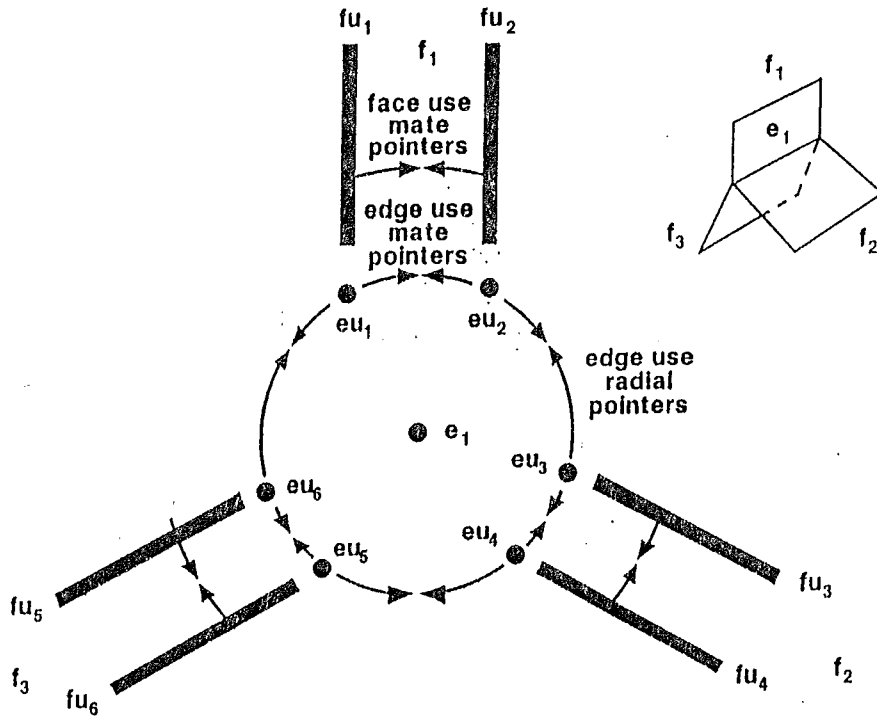


# Non-manifold topological representation



Radial Edge structure relationships





Plan view of a loop of edges in the Radial Edge structure

